Introduction

The main aim of the paper is to identify price fluctuations on the secondary housing market in the years 1996-2009 in Wrocław. The subject scope results from the aim of the paper and includes price fluctuations on the secondary housing market, involving both property rights and cooperative property rights for private accommodation. In this research only dwellings located in multifamily buildings are analyzed. The choice depends on two factors. Firstly, majority of dwellings are located just in multifamily buildings (blocks of flats – up to 90% in big Polish cities). Secondly, houses are characterized by a great differentiation regarding both quantitative and qualitative features, which requires that the data base should involve the appropriate information about each property in order to construct house price indexes. On the other hand the secondary housing market is greater than the primary market (approximately up to three times) taking into consideration the number of transactions.

The paper is divided into three parts. In the first part the time series components are analyzed. Then the methods of business cycles analysis are applied to house prices fluctuations on the local markets. The third part of the paper contains analysis of fluctuation of flats’ prices in Wrocław in the years 1996-2009.

1. Time series’ components

Empirical analyses the aim of which is to differentiate and characterize the changes occurring in macroeconomic variables are based on the assumption that the following elements may be distinguished in the structure of a time series\(^1\):

- trend component,
- seasonal component,
- cyclical component,

irregular component.

*Trend* is a long-time regular direction of changes (increase or decrease) of the value of examined variable. Trend can be used for object illustration of growth trend and facilitates retrospective description of examined factor in time. Trend is a result of operation of certain set of factors both objective and subjective ones, affecting examined variable.

*Seasonal fluctuations* are changes of intensity of economic activity that occur in one year time and which are the result of factors directly or indirectly depending on the year seasons. These fluctuations repeat regularly in one-year time and can be divided into two categories. The first type of seasonal fluctuations occurs in monthly, quarterly or half-year series and illustrates first of all an influence of year seasons and customs on economic activity. The second category of seasonal fluctuations are to be short-time oscillations that occur in one-month series. Their phases are presented within one day, twenty four hours, one week or one month. Main reasons for their occurrence are biological rhythm, customary division of labour, customs. In the majority of time series being subjects of economical analysis this type of fluctuations does not occur because examined series are available as monthly, quarterly, half-year or yearly data.

*Irregular fluctuations* result from indefinite chance causes that are not connected with the subject of the factor. Moreover, they are irregular when speaking both about their power and direction of activity. Main sources of these fluctuations are random events such as floods, draughts, earthquakes and political events such as wars and strikes.

*Cyclical fluctuations* are described as quite regularly repeated fluctuations, lasting more than one year and which are caused mainly by business cycle. Cyclical fluctuations result from economic factors, which makes difference between them and seasonal fluctuations.

Market of some goods, as well as the whole economy, fluctuate and mainly happen as consequences of business cycle. The same refers to property market. In time series of variables describing property market it is also possible to find trend, seasonal fluctuations, irregular fluctuations and cyclical fluctuations. These variables are the following: demand, supply and prices. Regarding prices on property market there can be: trend (in most cases trend is positive excluding Germany and Switzerland in 1975-2005 when real prices tended to decrease), seasonal fluctuations (increasing number of transactions during summer holidays), irregular fluctuations (decrease of flats’ prices on flooded areas in Wrocław in 1997) and cyclical fluctuations resulting from economic factors that have an influence on behaviours of this market participants.

2. Methodology of isolation of cyclical price fluctuations on the housing

In this paper the methods of business cycles analysis were applied to house prices fluctuations on the local markets. Plurality of methods of business cycle measurement makes it difficult to determine the turning points and cycle phases. According to accepted procedure external image of the cycle, locations of turning points as well as the duration of phases will vary. In this paper there have been imposed some methods of business cycle measurement that have their theoretical background in new classic macroeconomic concepts. According to

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R. E. Lucas⁶, business fluctuations are the set of moves around the trend determined by real GDP of the specific country. Such interpretation enables to measure the cycle as deviations from the trend. It is obvious that it refers only to business cycle. However, there are no obstacles to measure the subject of cyclical fluctuations for other economic variables identically. Then the trend will be searched within the series of variables other than GDP⁷.

Method of the cycle’s measurement as deviations from the trend is used very often but it isn’t the single one. Other basic methods of business cycle isolation are as follows: cycle of levels, cycle of growth, and cycle of deviations of growth rate from trend⁸. The first method abuts on estimations of fluctuations on the basis of absolute quantities of selected measuring instruments referring to the level of economic activity. The second method is based on growth dynamic. The last concept composes growth rates with long-time trend.

The first step to isolate cyclical fluctuations is to delete from the prime series seasonal and irregular fluctuations. The most popular and most often used methods of time series smoothing are X-12 ARIMA⁹ and TRAMO-SEATS. The first method was worked out by the U.S. Bureau of the Census and the other one by V. Gomez and A. Maravall¹⁰. These tools join classic decomposition of time series to components connected with trend, seasoning and irregular factor with modeling of time series with the use of ARIMA models. Smoothing of time series by using these methods enables to eliminate seasonal fluctuations and irregular factors from the series.

In the concept of deviations from the trend an essentials element is the way of determining the trend itself because a course of received fluctuations of market conditions is conditioned by the trend. Identification of cyclical oscillations with the use of this method is doubtful because of arbitrary choice of its function which may have an influence on final results. It has to be pointed out that this problem is connected with deterministic trend only¹¹. According to easiness of calculations and clear economic interpretation linear function is used most often. Using such deterministic trend amounts formally to finding the following equation:

\[ \hat{y}_t = \alpha_0 + \alpha_1 \times t + \varepsilon_t ; \]  

where:

\( \hat{y}_t \) – theoretical trend values for variable \( y \) in the time \( t \),
\( \alpha_0 \) – estimator of parameter of trend’s linear function defining a level of effects in the time \( t=0 \),
\( \alpha_1 \) – estimator of parameter of trend’s linear function defining an average increase of the value of effect in question,
\( \varepsilon_t \) – summand of remainder.

Assumption of linearity of trend’s function causes that any element disturbing formation of real property prices is of short-time character. It is assumed, however, that after some time an influence of disturbing factor will be neutralized and prices return to permanent growth line resulting from long-time linear trend. The most important factor of long-time

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changes of real estate’s prices are certainly changes in demand for property services. They depend mainly on economic situation of the economy thus tickling directly households – mainly their incomes and access to financing which is connected with mortgage loans rates. If we use linear function to describe trend of prices on real estate market, \( \alpha_1 \) estimator informs about an average price increase. Considering the fact that GDP cannot be recognized as permanent changing rate process an assumption of linear trend to separate fluctuations of real flat prices would not be proper. Furthermore, negation of linear function as good approximation for trend of macroeconomic variables results also from formal statistical reasons. Nelson and Plosser\(^{12}\) made empirical investigations that demonstrated that in the dynamic of the majority of time series exists random walk with drift. Then the formal entry of such course is as follows:

\[
y_t = \mu + y_{t-1} + \epsilon_t; \quad (2)
\]

where:

- \( y_t \) – empiric values \( y \) in the time \( t \),
- \( \epsilon_t \) – as in the equation,
- \( \mu \) – constant representing the drift (\( \mu > 0 \)).

Taking into consideration this element it can be stated that single disturbance of previous growth path will cause its permanent distortion. Acceptance of the thesis about formation of time series, as well as flats’ prices\(^{13}\), according to random walk with drift causes that the description of analyzed phenomenon with the use of linear trend is more and more complicated as it is changeable in time. It is more difficult to differentiate the trend from cyclical fluctuations as random walk causes that trend is also deviated\(^{14}\). Authors of the concept of real business cycle proposed statistical methods that can solve this problem. These methods are based on assumption that cyclical summand of variable \( y \) is a difference between its current value and a measure showing the value of the trend; the trend is weighted average of past, current and future observations\(^{15}\):

\[
y^c_t = y_t - \tau_t = \sum_{j=-J}^{J} a_j * y_{t-j}; \quad (3)
\]

where:

- \( y^c_t \) – cyclical summand of variable \( y \) in the time \( t \),
- \( \tau_t \) – stochastic (random) trend value.

This method, named the Hodrick-Prescott (HP) filter, allows calculating value \( \tau_t \), which minimize the expression:

\[
\sum_{t=1}^{T} (y_t - \tau_t)^2 + \lambda \sum_{i=2}^{T-1} [(\tau_{t+1} - \tau_t) - (\tau_t - \tau_{t-1})]^2; \quad (4)
\]

where:

- \( \lambda \) – smoothing parameter.

Smoothing parameter exposes various values depending on frequency of the phenomenon. If we have yearly data \( \lambda = 400 \), for quarterly data \( \lambda = 1600 \), and for monthly data


\(^{15}\) M. Kruszka, Synchronizacja wahań koniunkturalnych w gospodarce krajów rozwiniętych, Wiadomości Statystyczne 2003, nr 6, pp. 1-15.
λ=14400\textsuperscript{16}. The higher values of λ parameter, the more “flat” is the whole trend. It follows that if λ approaches infinity, using the filter we receive the same values as if we use linear trend \textsuperscript{17}. The most important limit of the presented filter is demanded minimal length of time serial that is being filtered. In practice minimal number of observations is 32.

The serial received after using the HP filter shows long-time growth tendency of the variable that is not deterministic function but is being changed itself in time. In order to isolate cyclical fluctuations empiric values of the variable should be divided by estimations received by using the HP filter (and multiplied by 100); then we received the serial showed percentage fluctuations from the trend\textsuperscript{18}.

3. Data used in the research

Flat prices indexes per square metre in Wrocław were constructed with a mix-adjustment method. From theoretical point of view the aim of this method is to define the pure change flat price. The data on asking prices used to construct flat price indexes were collected. As a result of methodological processes (repeated sales offers were omitted – this phenomenon of repeated offers was caused by reporting them to more than one agency.) the quantity of base data decreased half as much and amounted to 50000 in Wrocław. The number of collected offers satisfies the condition of representative sample. In the Diagram 1 nominal and real flat prices indexes in Wrocław in the years 1996-2009 are presented.

Diagram 1. Nominal and real flat price indexes in Wrocław in the years 1996-2009

Source: Based on own calculations.

The analysis of chart 1 shows that nominal flat price indexes in Wrocław increased by 540%, during the years 1996-2009. It is worth noticing that real flat price indexes in Wrocław increased by 210%. In both cities particularly rapid growth took place in the years 2006-2007.

\textsuperscript{18} In the situation when variables (free of seasoned fluctuations and any other chances) are logarithmed, in order to isolate cyclical fluctuations we should subtract empiric values of the variable by estimation resulted from use of the HP filter and multiply by 100.
According to prof. Bryx\textsuperscript{19} the rapid growth resulted from two factors. Firstly, the market was informed about the possibility of increasing V.A.T. (value addend tax) by 22%. Thus only those flats that were built just at that moment were burdened with 7% V.A.T. Secondly, the other important information was that the year 2006 was the last year to use tax relief. Taking into consideration the above mentioned facts it seems that rapid growth of demand met fixed supply and resulted in huge flat price growth in the year 2006.

4. Fluctuations of flat’ prices on housing markets in Wroclaw

Cyclical fluctuations of flat prices on the real estate market in Wroclaw were determined as deviations from the stochastic (random) trend. The very first step in the process of determination of the fluctuation was to make real (for the first quarter of 1996) flat price indexes in the years 1996-2009. Then the serial of real prices of 1 m\textsuperscript{2} of flat was decomposed into the following components:

- seasonal fluctuations,
- irregular fluctuations,
- fluctuations of both trend and cyclical,
- stochastic (random) trend.

Firstly, seasonal and irregular fluctuations were eliminated using X-12 ARIMA procedure. Basing on the final curve of fluctuations of both trend and cyclical (Henderson curve) there was estimated stochastic trend (with the use of the HP filter). It was the last stage of decomposition of analysed serial that enabled to determine cyclical fluctuations. The serial presenting cyclical fluctuations measured as a deviation cycle was determined by dividing the value of fluctuation of both trend and cyclical by proper values generated by the HP filter. Such serial was multiplied by 100\% to receive percentage deviations from the trend curve. Diagram 2 presents cyclical fluctuations of real flat prices index in Wroclaw in 1996-2008.

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{diagram2.png}
\caption{Cyclical fluctuations of real flat price index in Wroclaw in the years 1996-2009 \textit{Source:} Based on own calculations.}
\end{figure}

Fluctuations mentioned above were the basis for further analyses. The aim was to determine morphologic attributes of these fluctuations. It was assumed in the analysis that the

\textsuperscript{19} M. Bryx, Prawo do dachu nad głową, Problemy rozwoju miast 2007 nr 4, Instytut Rozwoju Miast, Kraków 2007
upper (lower) turning point appears in the period when the value of the analyzed indicator reaches its maximum (minimum). After establishing the turning points it was possible to differentiate the phases of the business cycles. Therefore, each cycle consists of an increase phase (between the lower and upper turning point) and a decrease phase (between the upper and lower turning point). Restrictions were imposed to ensure that the periods of increases and decreases had a minimum length of six quarters in order to avoid spurious cycles.\textsuperscript{20} Table 1 presents morphologic cyclical fluctuations of prices of 1 sq.m of flat attributes in Wroclaw in 1996-2009.

Table 1. Morphologic cyclical fluctuations of prices of 1m\textsuperscript{2} of flat in Wroclaw in 1996-2009

<table>
<thead>
<tr>
<th>Attributes of cycle</th>
<th>Phases of cyclical fluctuations</th>
<th>Within the time</th>
<th>Length in quarters</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>increasing</td>
<td>decreasing</td>
<td>increasing</td>
</tr>
<tr>
<td>III 2002</td>
<td></td>
<td>6</td>
<td>5</td>
</tr>
</tbody>
</table>

Source: Based on own calculations.

In 1996 -2009 it was possible to observe five phases of cyclical fluctuations on the secondary real estate market in Wroclaw – three increasing phases and two decreasing one that made two full cycle. Flat price cycle in Wroclaw took place from the third quarter of the year 1996 to the third quarter of the year 2002. The length of this cycle amounts to 24 quarters consisting of increasing phase of 16 quarters and decreasing phase of 9 quarters. The decreasing phase of the next cycle started in the third quarter of the year 2007.

References


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